

Rough-Fuzzy Classification with Two Thresholds- Algorithms and Implementations using C

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Abstract: In this paper, we propose three algorithms to index the records of a decision table with fuzzy decision attributes using two thresholds under Rough Computing. These algorithms are also implemented using C.

Keywords: Decision Table, Fuzzy Decision attributes, Rough Computing, Indexing.

1. Introduction

Z.Pawlak's rough sets [6,7,8] and L.Zadeh's fuzzy concepts [4] are widely in use in the area of knowledge engineering and hence, the hybridization of these two concepts is being focused by several researchers. In this line, G.Ganesan et. al., [1,2,3,5] introduced indexing techniques on the elements of the Universe of discourse through fuzzy a fuzzy subset using rough tools. In this paper, we worked on these contributions and developed the algorithms of three types of indices namely **lower**, **upper** and **rough** and implemented them using C Programming. The paper is organized into 6 sections. In section 2, the basic mathematical concepts pertained to the subsequent sections are dealt. In 3rd, 4th and 5th sections we provide lower, upper and rough indices algorithms respectively for a decision table with fuzzy decision attribute using two thresholds and these algorithms are implemented using C Programming. The 6th section deals with the concluding remarks.

2. Mathematical Preliminaries

Here, we describe the mathematical concepts involved in the subsequent sections.

2.1 Rough Sets

For a given finite universal set U and an equivalence relation R , let $U/R = \{W_1, W_2, \dots, W_m\}$ denote the quotient space of U induced by R . For a given subset A of U , the lower and upper rough approximations [7,8] proposed by Z.Pawlak may be obtained by the following algorithms.

Lower Rough Approximations

$\parallel W_1, W_2, \dots, W_m$ – Equivalence Classes

$\parallel A$ – Input

Let $D = \text{NULL}$

For $i=1$ to m do

If W_i is subset of A , then $D = D \cup W_i$

Return D

Lower Rough Approximations

// W_1, W_2, \dots, W_m – Equivalence Classes

// A-Input

Let $D = \text{NULL}$

For $i=1$ to m do

If $A \cap W_i \neq \text{NULL}$ then $D = D \cup W_i$

Return D

2.2 Hybridization of Roughness and fuzziness through two thresholds

For a given Universal set U , let A be any fuzzy subset of U and let α and β denote two thresholds ($\alpha < \beta$) ranging between 0 and 1. Define $A[\alpha, \beta] = \{x \in U / \alpha < \mu_A(x) < \beta\}$. The lower and upper rough approximations of A with respect to α and β are given by $A_{\alpha, \beta} = \underline{A}[\alpha, \beta]$ and $A^{\alpha, \beta} = \overline{A}[\alpha, \beta]$ respectively.

3. Lower Indices in a Decision Table with Fuzzy Decision Attribute

Here, an algorithm is dealt to compute the lower index by using square and square root functions on two thresholds of a fuzzy input A . To compute the index, the lower rough approximations are used. This algorithm is illustrated using a decision table with fuzzy decision attribute.

3.1 Algorithm for Lower index of an element

Algorithm (alpha, beta, A, x)

//Algorithm to obtain index of x an element of universe of discourse

//Algorithm returns the index

1. Let x_index be an integer initialized to M .
2. Pick the equivalence class K containing x .
3. If $U(y)=0$ for all y belongs to K
 - Begin
 - $x_index = -x_index$
 - goto 7
 - End
4. If $U(y)=1$ for all y belongs to K
 - goto 7
5. Compute “A lower bound of alpha,beta”

6. If “ x belongs to A lower bound of alpha,beta”

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While (“x belongs to A lower bound of alpha,beta”)
  Begin
  alpha= sqrt(alpha) //square root of alpha
  beta = sqrt(beta) //square of beta
  x_index=x_index+1
  Compute “A lower bound of alpha,beta”
  End

```

else

```

While (“x NOT belongs to A lower bound of alpha,beta”)
  Begin
  alpha= sqrt(alpha) //square of alpha
  beta = sqrt(beta) // square root of beta
  x_index=x_index-1
  Compute “A lower bound of alpha,beta”
  End

```

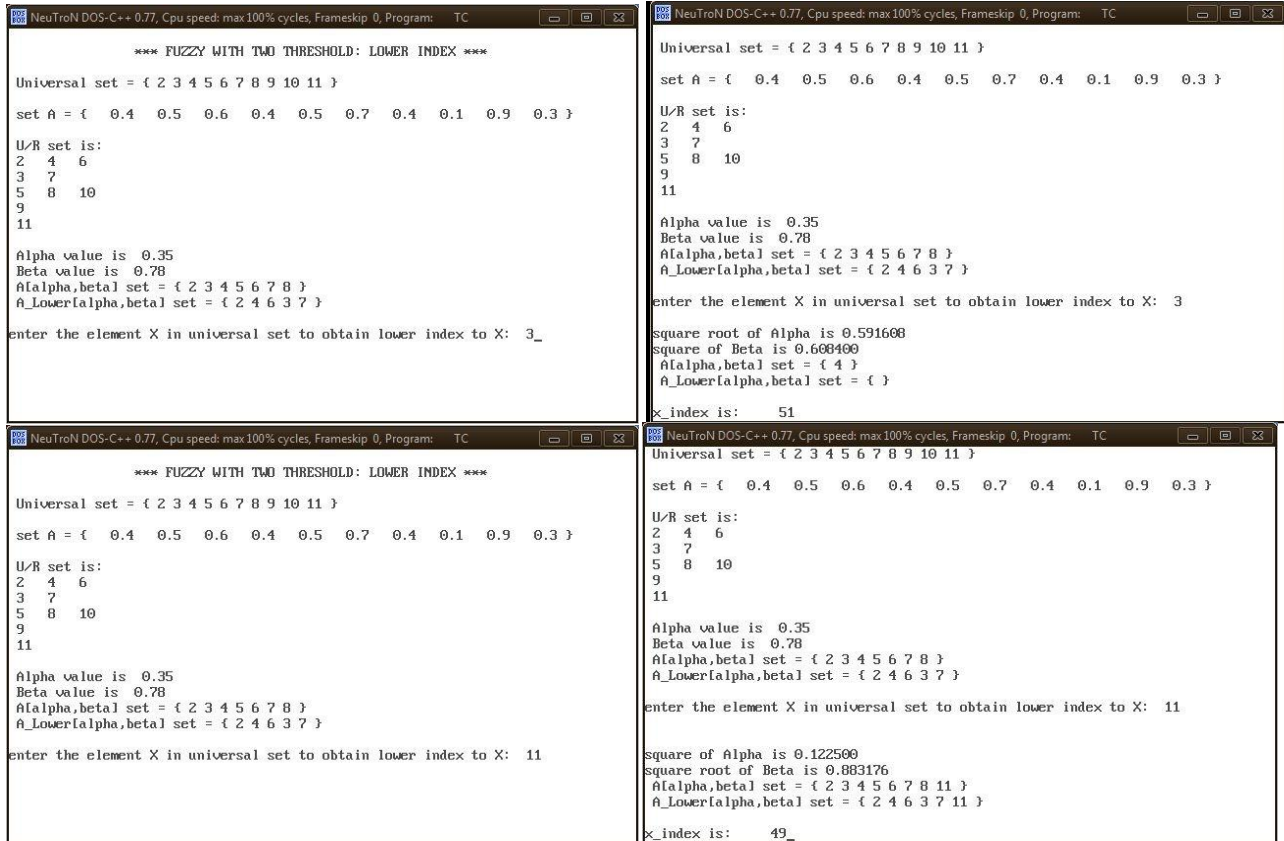
7. Return x_index

3.2 Experimental Results

Consider the following decision table with 10 records namely 2,3,4,5,6,7,8,9,10 and 11 with three conditional attributes namely Attr_1, Attr_2, Attr_3 and a fuzzy decision attribute.

	Attr_1	Attr_2	Attr_3	Decision
2	Excellent	Good	Excellent	0.4
3	Good	Excellent	Very Good	0.5
4	Good	Good	Excellent	0.6
5	Poor	Very Good	Fair	0.4
6	Fair	Good	Fair	0.5
7	Poor	Excellent	Good	0.7
8	Excellent	Very Good	Fair	0.4
9	Excellent	Fair	Poor	0.1
10	Very Good	Very Good	Good	0.9
11	Fair	Poor	Fair	0.3

It may be noticed that the records are grouped according the similarity for each key or group of keys. i.e., the records are grouped as follows: For Attr_1, the grouping are {(Excellent, {2,8,9}), (Very Good,{10}), (Good, {3,4}), (Fair, 6,11)}, (Poor, {5,7}) }. For Attr_2, the grouping are {(Excellent,{3,7}), (Very Good,{5,8,10}), (Good,{2,4,6}), (Fair,{9}), (Poor,{11})} and for Attr_3, we obtain {(Excellent, {2,4}), (Very Good,{3}), (Good,{7,10}), (Fair,{5,6,8,11}), (Poor,{9})}. The above example is implemented in C by using Attr_2 as the key and the threshold as 0.35 using the thresholds as 0.35 and we obtain the lower index of 3 as 51 and the lower index of 11 as 49



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*** FUZZY WITH TWO THRESHOLD: LOWER INDEX ***

Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A[alpha,beta] set = { 2 3 4 5 6 7 8 }
A_Lower[alpha,beta] set = { 2 4 6 3 7 }

enter the element X in universal set to obtain lower index to X: 3_

Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A[alpha,beta] set = { 2 3 4 5 6 7 8 }
A_Lower[alpha,beta] set = { 2 4 6 3 7 }

enter the element X in universal set to obtain lower index to X: 3

square root of Alpha is 0.591608
square of Beta is 0.608400
A[alpha,beta] set = { 4 }
A_Lower[alpha,beta] set = { }
x_index is: 51

*** FUZZY WITH TWO THRESHOLD: LOWER INDEX ***

Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A[alpha,beta] set = { 2 3 4 5 6 7 8 }
A_Lower[alpha,beta] set = { 2 4 6 3 7 }

enter the element X in universal set to obtain lower index to X: 11

Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A[alpha,beta] set = { 2 3 4 5 6 7 8 }
A_Lower[alpha,beta] set = { 2 4 6 3 7 }

enter the element X in universal set to obtain lower index to X: 11

square of Alpha is 0.122500
square root of Beta is 0.883176
A[alpha,beta] set = { 2 3 4 5 6 7 8 11 }
A_Lower[alpha,beta] set = { 2 4 6 3 7 11 }
x_index is: 49_
  
```

4. Upper Indices in a Decision Table with Fuzzy Decision Attribute

In this section, we propose an algorithm to compute index using upper rough approximations. Similar to third section, square and square root functions are used on two thresholds of a fuzzy input A. The algorithm is illustrated with a decision table consisting of a fuzzy decision attribute.

4.1 Algorithm for Upper index of an element (in Fuzzy Two threshold):-

Algorithm (alpha, A, x)

//Algorithm to obtain index of x an element of universe of discourse

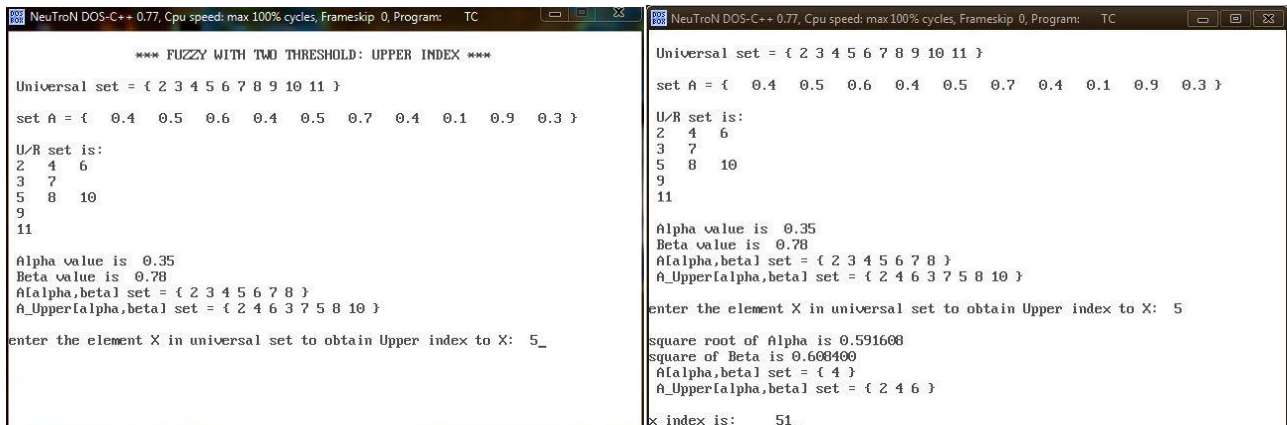
//Algorithm returns the index

1. Let x_index be an integer initialized to M.
2. Pick the equivalence class K containing x.
3. If $U(y)=0$ for all y belongs to K
 Begin
 x_index = -x_index
 goto 7
 End
4. If $U(y)=1$ for all y belongs to K
 goto 7

5. Compute “A upper bound of alpha, beta”
6. If “x belongs to A upper bound of alpha, beta”
 - While (“x belongs to A upper bound of alpha, beta”)
 - Begin
 - alpha = sqrt(alpha) //square root of alpha
 - beta = sqr(beta)
 - x_index=x_index+1
 - Compute “A upper bound of alpha”
 - End
 - else
 - While (“x NOT belongs to A upper bound of alpha, beta”)
 - Begin
 - alpha= sqr(alpha) //square of alpha
 - beta = sqrt(beta)
 - x_index=x_index-1
 - Compute “A upper bound of alpha”
 - End
7. Return x_index

4.2 Experimental Results

The above algorithm is implemented in C by considering the example as quoted for lower index, and we obtain the upper index of 5 as 51 and 9 as 48



```

*** FUZZY WITH TWO THRESHOLD: UPPER INDEX ***
Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A_alpha,beta set = { 2 3 4 5 6 7 8 }
A_Upper[alpha,beta] set = { 2 4 6 3 7 5 8 10 }
enter the element X in universal set to obtain Upper index to X: 5_

Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A_alpha,beta set = { 2 3 4 5 6 7 8 }
A_Upper[alpha,beta] set = { 2 4 6 3 7 5 8 10 }
enter the element X in universal set to obtain Upper index to X: 5
square root of Alpha is 0.591608
square of Beta is 0.608400
A_alpha,beta set = { 4 }
A_Upper[alpha,beta] set = { 2 4 6 }
x_index is: 51_
  
```

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*** FUZZY WITH TWO THRESHOLD: UPPER INDEX ***
Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A[alpha,beta] set = { 2 3 4 5 6 7 8 }
A_Upper[alpha,beta] set = { 2 4 6 3 7 5 8 10 }
enter the element X in universal set to obtain Upper index to X: 9

square of Alpha is 0.122500
square root of Beta is 0.883176
A[alpha,beta] set = { 2 3 4 5 6 7 8 11 }
A_Upper[alpha,beta] set = { 2 4 6 3 7 5 8 10 11 }

square of Alpha is 0.015006
square root of Beta is 0.939775
A[alpha,beta] set = { 2 3 4 5 6 7 8 9 10 11 }
A_Upper[alpha,beta] set = { 2 4 6 3 7 5 8 10 9 11 }
x_index is: 48_
  
```

5. Rough Indices in a Decision Table with Fuzzy Decision Attribute

By hybridizing the lower and upper rough approximations, in this section we propose an algorithm to compute rough indices by squaring or square rooting two thresholds of the given fuzzy input A. The algorithm is demonstrated with a decision table containing a fuzzy decision attribute.

5.1 Algorithm for Rough index of an element

Algorithm (alpha, beta, A, x)

//Algorithm to obtain index of x an element of universe of discourse

//Algorithm returns the index

1. Let x_index be an integer initialized to M
2. Pick the equivalence class K containing x.
3. If $U(y)=0$ for all y belongs to K
 Begin
 x_index = -x_index
 goto 8
 End
4. If $U(y)=1$ for all y belongs to K
 goto 8
5. Compute “A lower bound of alpha, beta”, “A upper bound of alpha, beta”
6. If “x belongs to A lower bound of alpha, beta”
 While (“x belongs to A lower bound of alpha, beta”)
 Begin
 alpha= sqrt(alpha) //square root of alpha
 beta = sqr(beta) // square of beta
 x_index=x_index+1
 Compute “A lower bound of alpha, beta”
 End
 Goto 8

else

7. If “x NOT belongs to A upper bound of alpha, beta”

While (“x NOT belongs to A upper bound of alpha, beta”)

Begin

alpha= sqrt(alpha) //square of alpha

beta = sqrt(beta) // square root of beta

x_index=x_index-1

Compute “A upper bound of alpha,beta”

End

else

Begin

Gamma=alpha

Delta=beta

compute “A lower bound of alpha,beta” , “A upper bound of gamma, delta”

while(“x NOT belongs to A lower bound of alpha, beta” AND

“x belongs to A upper bound of gamma, delta”)

Begin

alpha = sqrt(alpha) //square root of alpha

beta = sqrt(beta) //square of beta

gamma=sqrt(gamma) //square root of gamma

delta=sqr(delta) // square of delta

compute “A lower bound of alpha, beta” , “A upper bound of gamma, delta”

x_index=x_index+1

End

If “x belongs to A lower bound of alpha, beta”

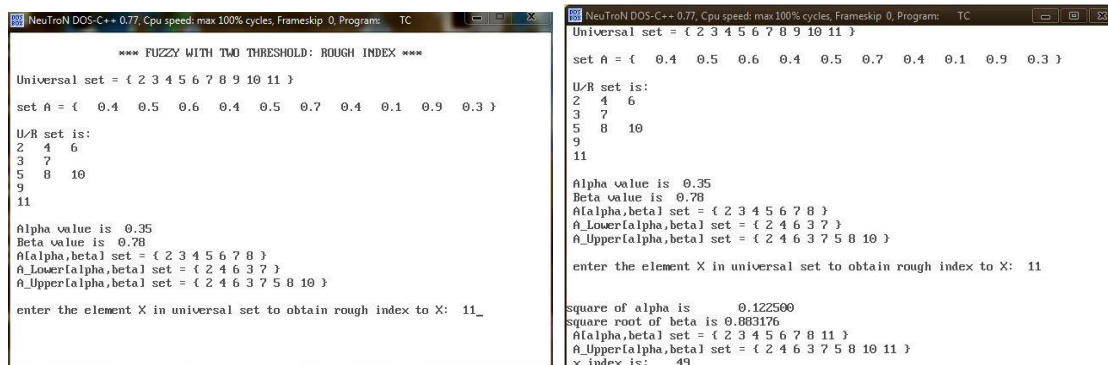
x_index=-x_index

End

8. Return x_index

5.2 Experimental Results

The above algorithm is implemented in C by considering the example as quoted for lower index, and we obtain the rough indices of 7 and 11 as 51 and 49 respectively.



```

*** FUZZY WITH TWO THRESHOLD: ROUGH INDEX ***
Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A_alpha,beta set = { 2 3 4 5 6 7 8 }
A_Lower(alpha,beta) set = { 2 4 6 3 7 }
A_Upper(alpha,beta) set = { 2 4 6 3 7 5 8 10 }
enter the element X in universal set to obtain rough index to X: 11_

Universal set = { 2 3 4 5 6 7 8 9 10 11 }
set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }
U/R set is:
2 4 6
3 7
5 8 10
9
11
Alpha value is 0.35
Beta value is 0.78
A_alpha,beta set = { 2 3 4 5 6 7 8 }
A_Lower(alpha,beta) set = { 2 4 6 3 7 }
A_Upper(alpha,beta) set = { 2 4 6 3 7 5 8 10 }
enter the element X in universal set to obtain rough index to X: 11
square of alpha is 0.122500
square root of beta is 0.883176
A_alpha,beta set = { 2 3 4 5 6 7 8 11 }
A_Upper(alpha,beta) set = { 2 4 6 3 7 5 8 10 11 }
x_index is: 49
  
```

```

*** FUZZY WITH TWO THRESHOLD: ROUGH INDEX ***

Universal set = { 2 3 4 5 6 7 8 9 10 11 }

set A = { 0.4 0.5 0.6 0.4 0.5 0.7 0.4 0.1 0.9 0.3 }

U/R set is:
2 4 6
3 7
5 8 10
9
11

Alpha value is 0.35
Beta value is 0.78
A_alpha,beta set = { 2 3 4 5 6 7 8 }
A_Lower_alpha,beta set = { 2 4 6 3 7 }
A_Upper_alpha,beta set = { 2 4 6 3 7 5 8 10 }

enter the element X in universal set to obtain rough index to X: 7

square root of alpha is 0.000000
square of beta is 0.780000
A_alpha,beta set = { 4 7 }
A_Lower_alpha,beta set = { }
x_index is: 51
  
```

6. Conclusion

In this paper, through C, we implemented the algorithms which were proposed to index a decision table using rough approximations. The same approach may be further extended for any information system with fuzzy decision attributes.

References

1. B.Krishnaveni, V.Syamala, D.Latha, G.Ganesan; Characterization of Information Systems with Fuzzy and Intuitionistic Fuzzy Decision Attributes, 8th International Conference on Advanced Software Engineering & Its Applications, 2015, Korea, pp: 53-58, IEEE, 2015
2. D.Latha, D.Rekha, K.Thangadurai, G.Ganesan; Probabilistic Rough Classification in Information Systems with Fuzzy Decision Attributes, International Journal on Recent and Innovation Trends in Computing and Communication, Vol:1 Issue: 6, pp: 547-552, 2013
3. G.Ganesan, et.al.; Rough Index in Information System with Fuzziness in Decision Attributes, International journal of Fuzzy Mathematics, Vol: 17, No: 1, pp: 183-190, 2008
4. Ganesan G, et.al., Feature Selection using Fuzzy Decision Attributes, Journal of INFORMATION, Vol 9, No3, pp:381-394, 2006
5. Ganesan G et.al., Rough Set: Analysis of Fuzzy Sets using thresholds, Computational Mathematics, Narosa, India, pp: 81-87, 2005
6. Ganesan G, et.al., An overview of rough sets, proceedings of the National Conference on the emerging trends in Pure and Applied Mathematics, Palayamkottai, India, pp: 70-76, 2005
7. Zdzislaw Pawlak, Rough Sets-Theoretical Aspects and Reasoning about Data, Kluwer Academic Publications, 1991
8. Zdzislaw Pawlak, Rough sets, International Journal of Computer and Information Sciences, 11, 341-356, 1982.